

Comisión Interamericana del Atún Tropical  
Inter-American Tropical Tuna Commission



# Introduction to the spatiotemporal model: VAST

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# Background of VAST

- R package developed and maintained by Jim Thorson (AFSC)
- How to install: `install_github("james-thorson/VAST")`
- Built based upon a previous R package: SpatialDeltaGLMM
- Spatial delta-generalized linear mixed model for multiple categories (species, size, or age classes): separately models encounter probability and positive catch rate
- Well documented with user manual and examples provided (<https://github.com/James-Thorson/VAST>)
- Very flexible model framework with detailed guidance regarding major decisions provided (<https://doi.org/10.1016/j.fishres.2018.10.013>)
- Has been used to standardize the catch rate of the dolphin-associated yellowfin fishery in the EPO (<https://doi.org/10.1016/j.fishres.2019.01.013>)

# Model Structure (single species)

VAST separately models encounter probability ( $p$ ) and positive catch rate ( $\lambda$ ) for each catch rate observation  $i$ :

$$\text{logit}(p_i) = \beta_1(t_i) + L_{\omega_1}\omega_1(s_i) + L_{\varepsilon_1}\varepsilon_1(s_i, t_i) + L_{\delta_1}\delta_1(v_i) + \sum_{k=1}^{n_k} \lambda_1(k)Q(i, k) + \sum_{p=1}^{n_p} \gamma_1(p)X(s_i, t_i, p)$$

$$\log(\lambda_i) = \beta_2(t_i) + L_{\omega_2}\omega_2(s_i) + L_{\varepsilon_2}\varepsilon_2(s_i, t_i) + L_{\delta_2}\delta_2(v_i) + \sum_{k=1}^{n_k} \lambda_2(k)Q(i, k) + \sum_{p=1}^{n_p} \gamma_2(p)X(s_i, t_i, p)$$

$\beta(t_i)$ : intercept in year  $t_i$

$\omega(s_i)$ : spatial variation at location  $s_i$ ;  $L_{\omega}$ : scaling factor (sd)

$\varepsilon(s_i, t_i)$ : spatiotemporal variation at location  $s_i$  in year  $t_i$ ;  $L_{\varepsilon}$ : scaling factor (sd)

$\delta(v_i)$ : vessel/targeting effects on catchability;  $L_{\delta}$ : scaling factor (sd)

$Q(i, k)$ : catchability covariate(s);  $\lambda(k)$ : associated catchability parameter(s)

$X(s_i, t_i, p)$ : habitat covariate(s);  $\gamma(p)$ : associated habitat parameter(s)

# Correlated spatial and spatiotemporal variations

Correlated spatial and spatiotemporal variations:

$$\omega_1 \sim \text{MVN}(\mathbf{0}, \mathbf{R}_1)$$

$$\omega_2 \sim \text{MVN}(\mathbf{0}, \mathbf{R}_2)$$

$$\varepsilon_1(t) \sim \text{MVN}(\mathbf{0}, \mathbf{R}_1)$$

$$\varepsilon_2(t) \sim \text{MVN}(\mathbf{0}, \mathbf{R}_2)$$

where

$$\mathbf{R}_1(s, s') = \frac{1}{2^{\nu-1}\Gamma(\nu)} \times (\kappa_1 |\mathbf{H}(s - s')|)^{\nu} \times K_{\nu}(\kappa_1 |\mathbf{H}(s - s')|)$$

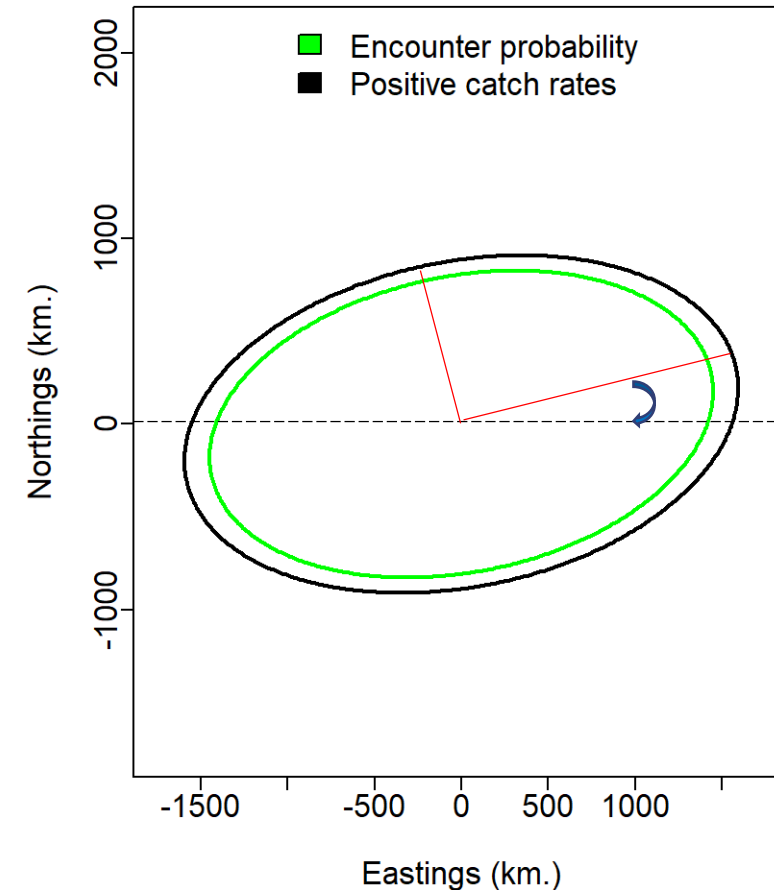
$$\mathbf{R}_2(s, s') = \frac{1}{2^{\nu-1}\Gamma(\nu)} \times (\kappa_2 |\mathbf{H}(s - s')|)^{\nu} \times K_{\nu}(\kappa_2 |\mathbf{H}(s - s')|)$$

decorrelation  
distance

geometric  
anisotropy

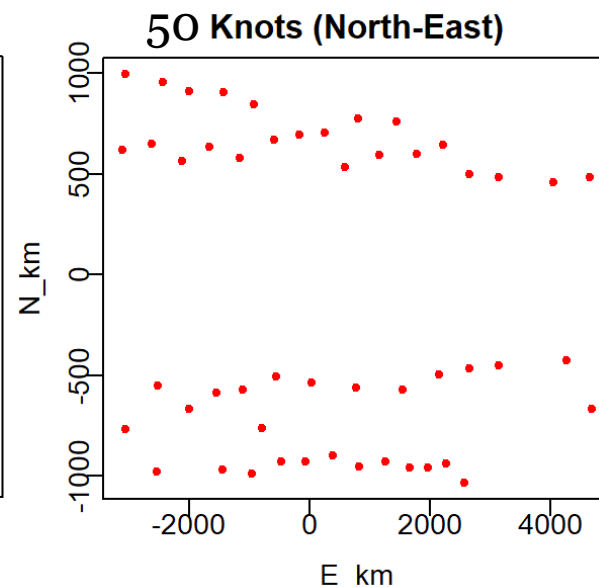
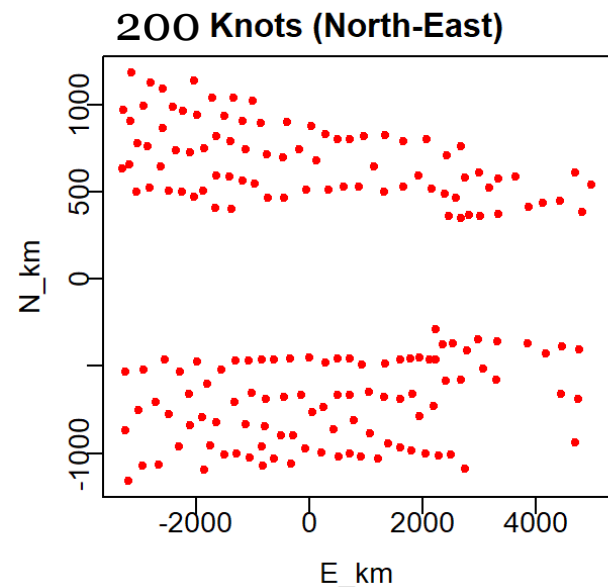
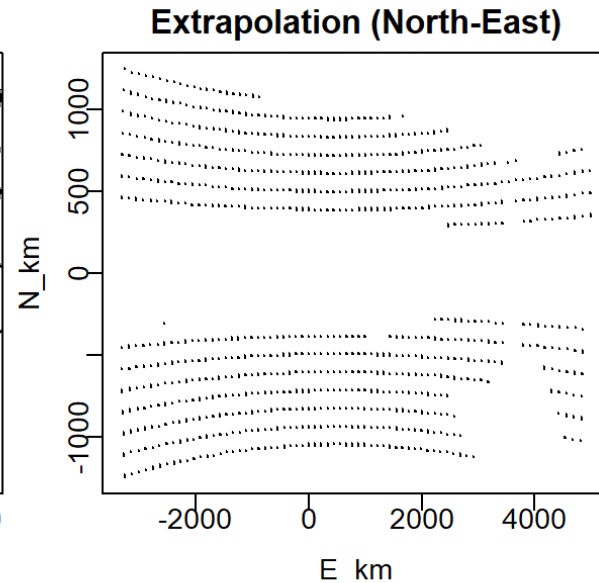
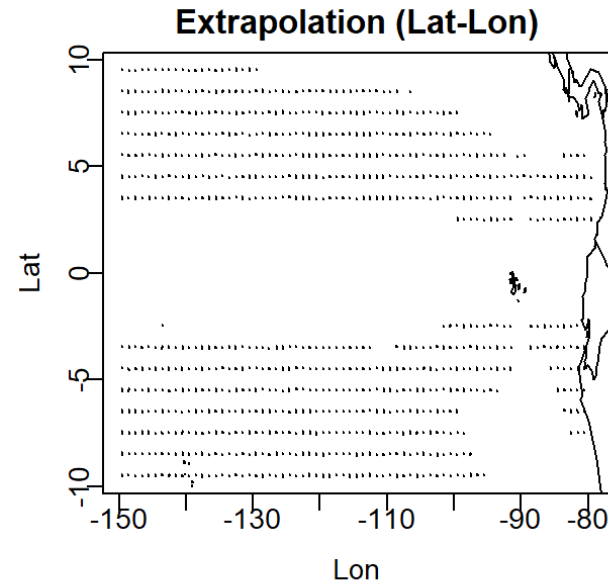
Matérn  
smoothness

Distance at 10% correlation



# Model assumptions

- To increase computation efficiency, VAST groups all sample locations into a user-specified number of knots
- Assumption: the spatial/spatiotemporal variation associated with a knot is constant within every time step
- Trad-off: high estimation accuracy (a large number of knots) vs. high computation efficiency (a small number of knots)



# Model Structure

The probability of catch data  $c$  for sample  $i$ :

$$\Pr(c_i = c) = \begin{cases} 1 - p_i & \text{if } c = 0 \\ p_i \times \text{Lognormal}(c_i | \log(\lambda_i), \sigma_m^2) & \text{if } c > 0 \end{cases}$$

**Standardized index is computed using an area-weighted approach:**

$$I(t) = \sum_{k=1}^{n_k} (\text{area}(k) \times \text{density}(k, t))$$

where  $\text{density}(k, t) = \text{logit}^{-1} \left( \beta_1(t_k) + L_{\omega_1} \omega_1(s_k) + L_{\varepsilon_1} \varepsilon_1(s_k, t_k) + \sum_{p=1}^{n_p} \gamma_1(p) X(s_i, t_i, p) \right) \times \exp \left( \beta_2(t_k) + L_{\omega_2} \omega_2(s_k) + L_{\varepsilon_2} \varepsilon_2(s_k, t_k) + \sum_{p=1}^{n_p} \gamma_2(p) X(s_i, t_i, p) \right)$

\*\*\* Vessel/targeting effects ( $\delta$ ) and catchability covariates ( $Q$ ) are both excluded (set to be 0) in the computation of local density: **index is proportional to abundance**

# Flexible model framework

- Turn on (1) or turn off (0) spatial and spatiotemporal components for encounter probability and positive catch rate

**FieldConfig = c("Omega1"=1, "Epsilon1"=1, "Omega2"=1, "Epsilon2"=1)**

- Specify the temporal structure for each component (fixed effect, independent, random walk, or autoregressive)

**RhoConfig = c("Beta1"=0, "Beta2"=0, "Epsilon1"=0, "Epsilon2"=0)**

- With (1) and without (0) vessel/targeting effects for encounter probability and positive catch rate

**OverdispersionConfig = c(0,0)**

- Other link functions for encounter probability and positive catch rate are available

**ObsModel = c(1,1)**

# Case study: dolphin-associated EPO yellowfin fishery

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## Spatiotemporal dynamics of the dolphin-associated purse-seine fishery for yellowfin tuna (*Thunnus albacares*) in the eastern Pacific Ocean

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### ABSTRACT

Spatiotemporal models of catch rate data are used in fisheries science to understand the spatiotemporal dynamics of a fishery and, more importantly, to produce a standardized index of relative abundance for stock assessment models. Here, we apply a spatiotemporal delta-generalized linear mixed model to catch rate data

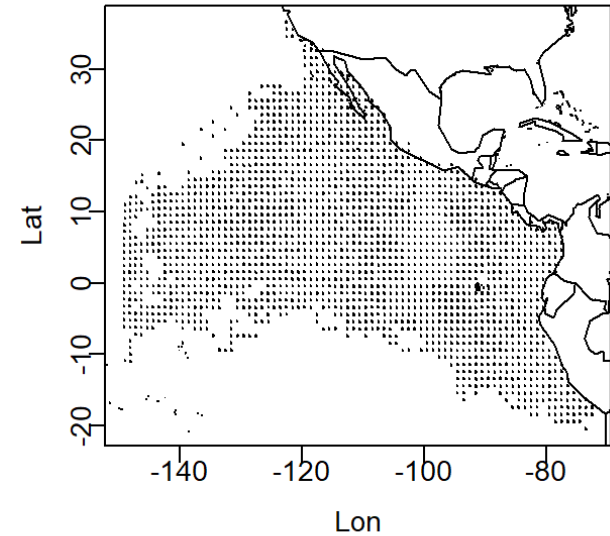




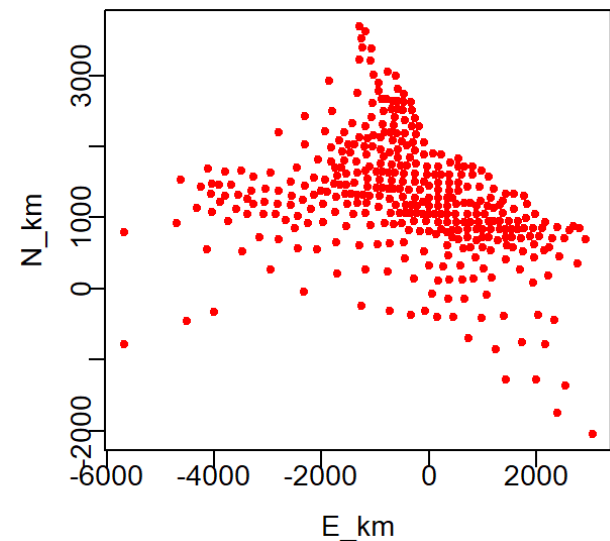
# Step 1. Define the spatial domain and “knots”



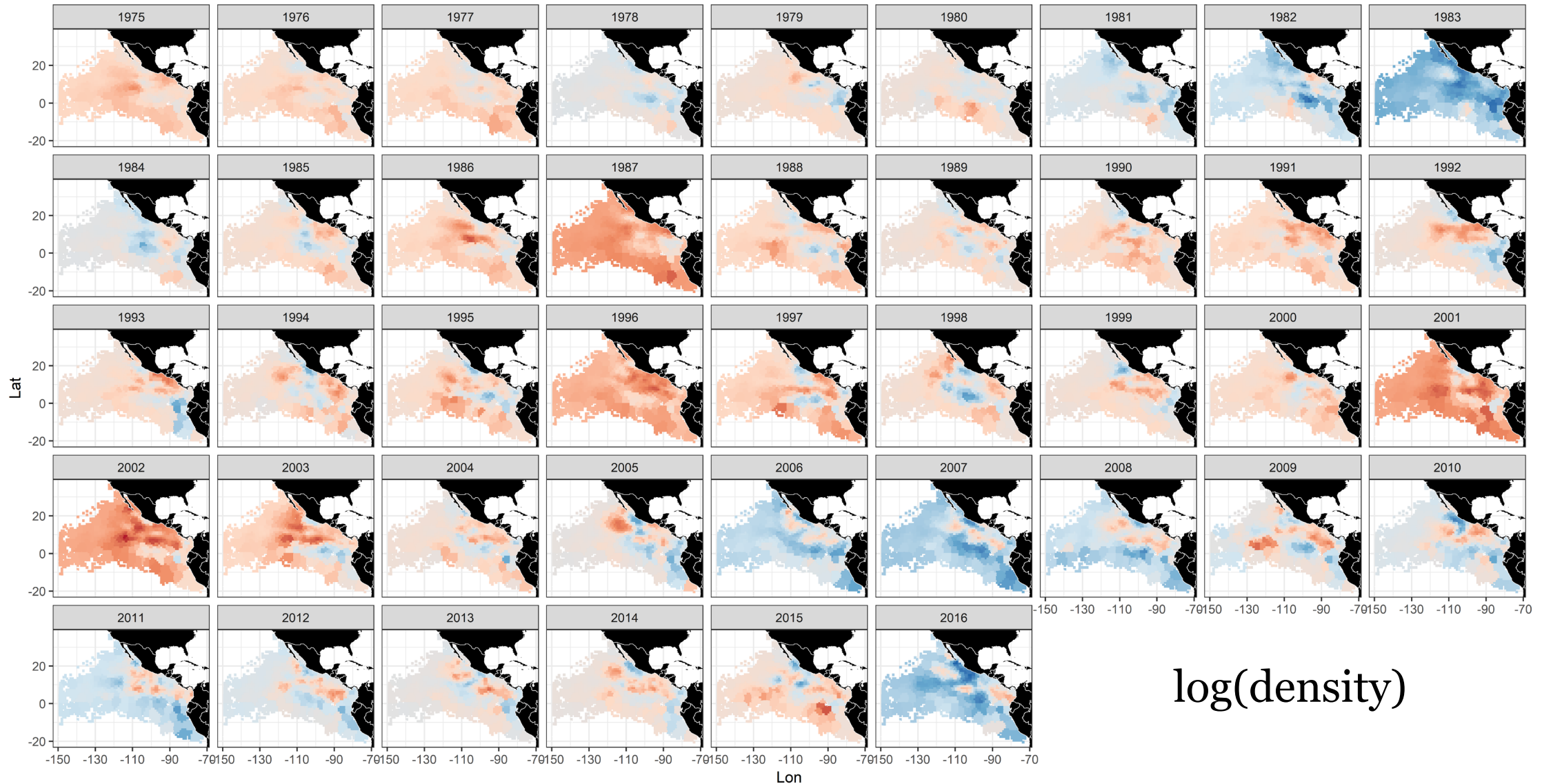
Extrapolation (Lat-Lon)



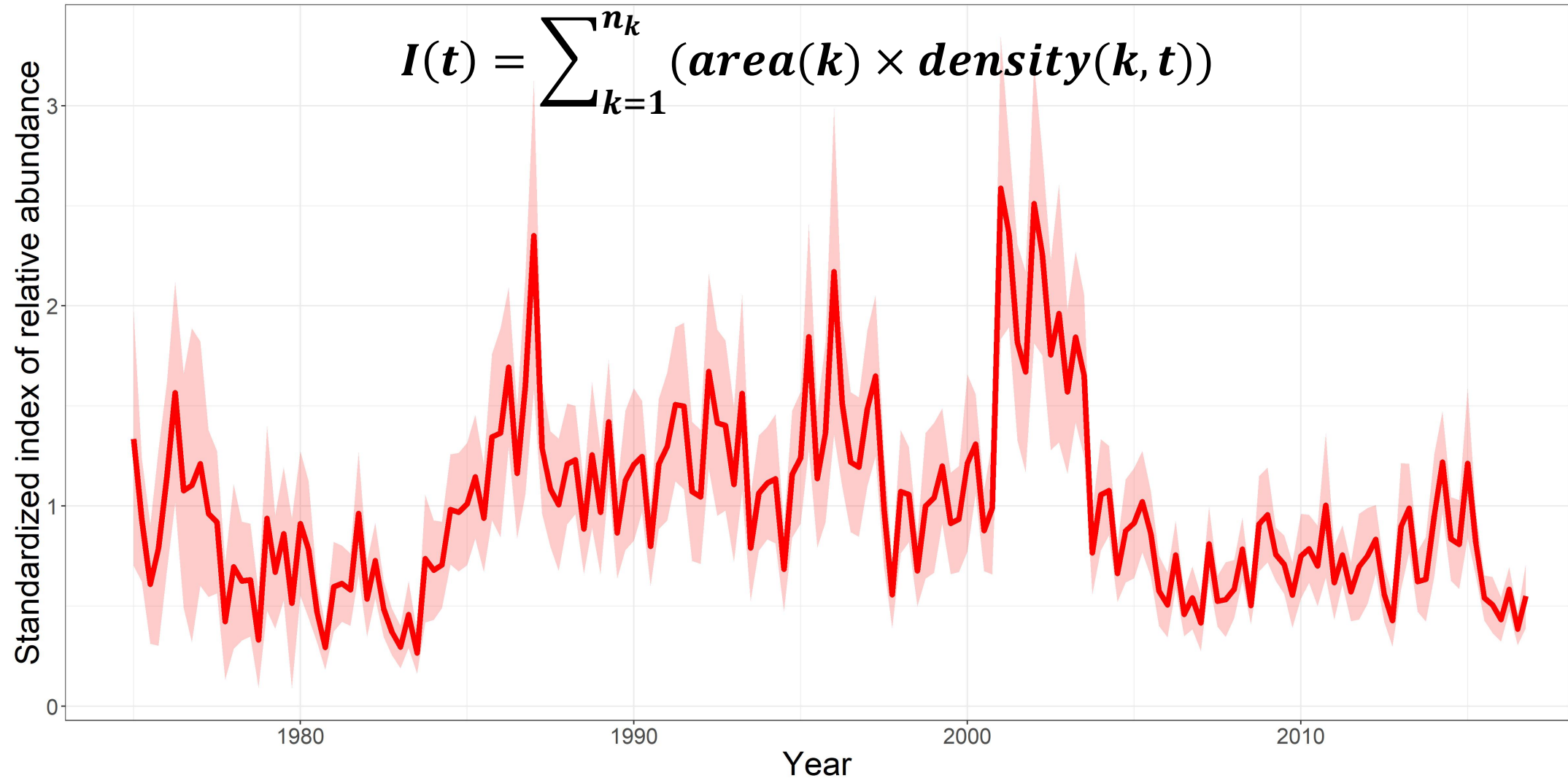
Knots (North-East)



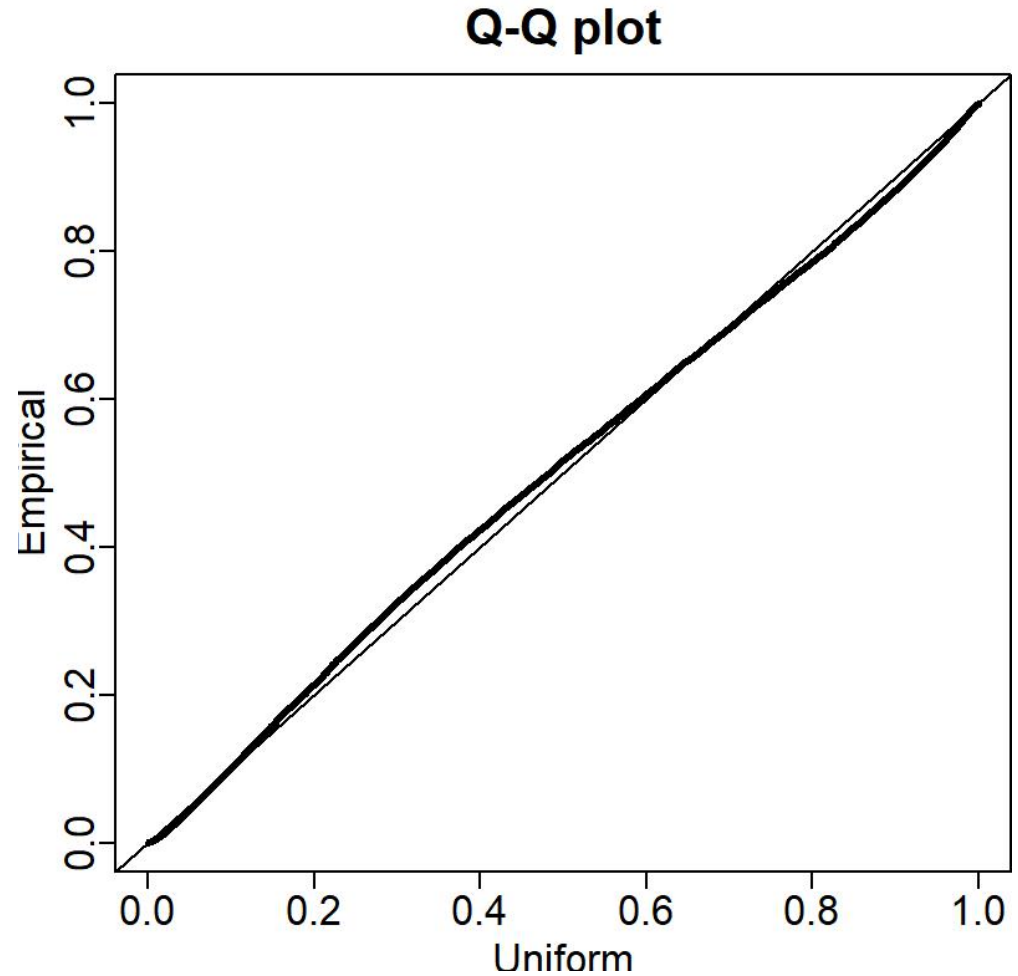
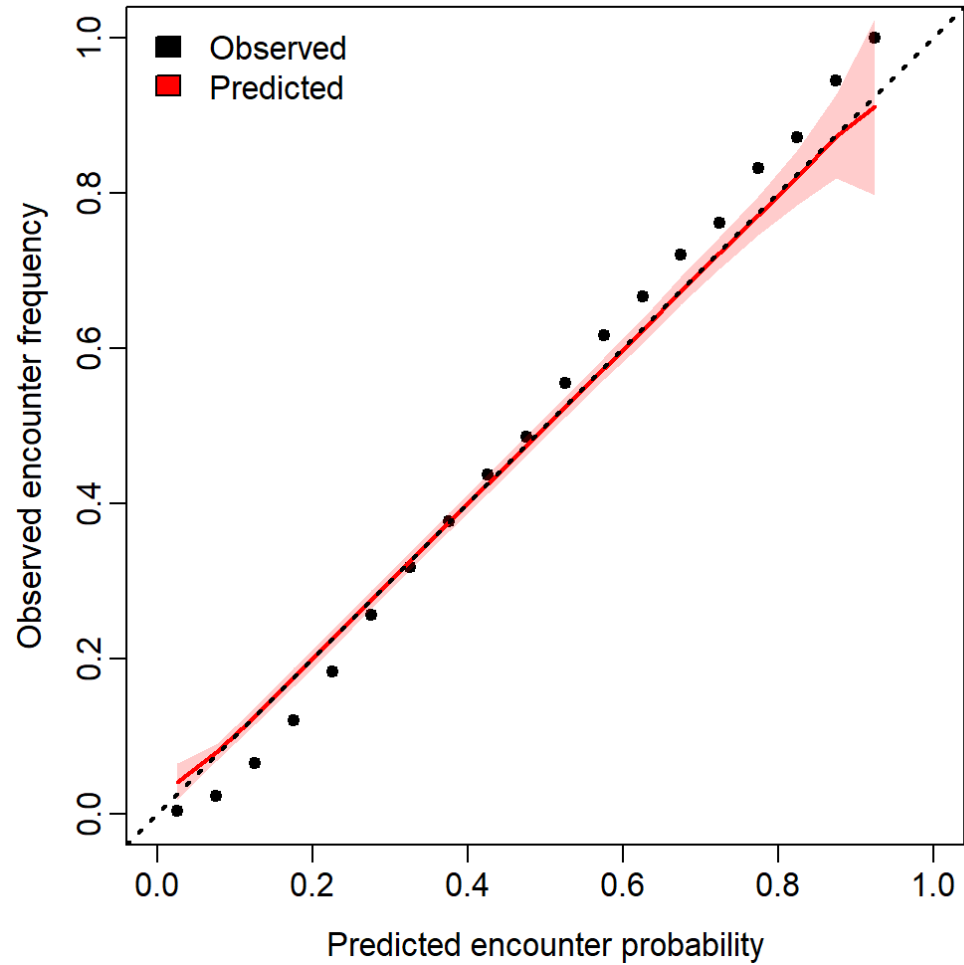
# Step 2. Predict density for every year and knot



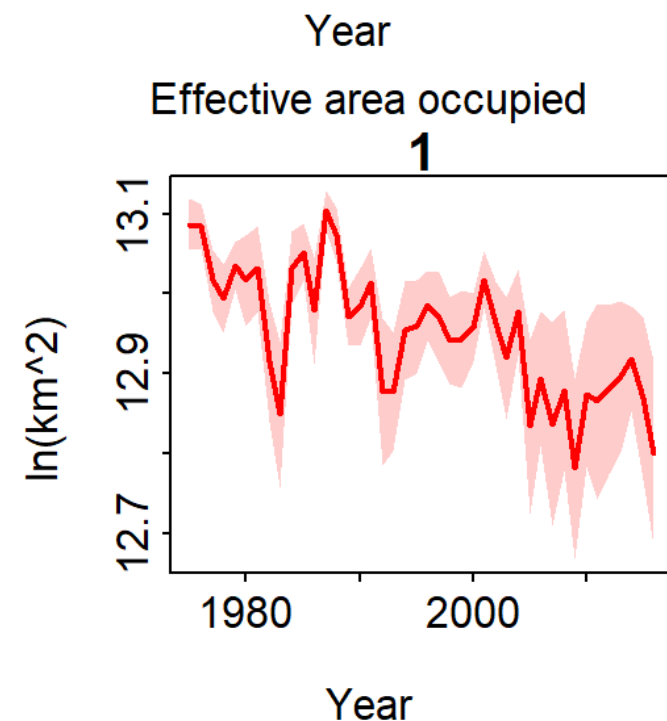
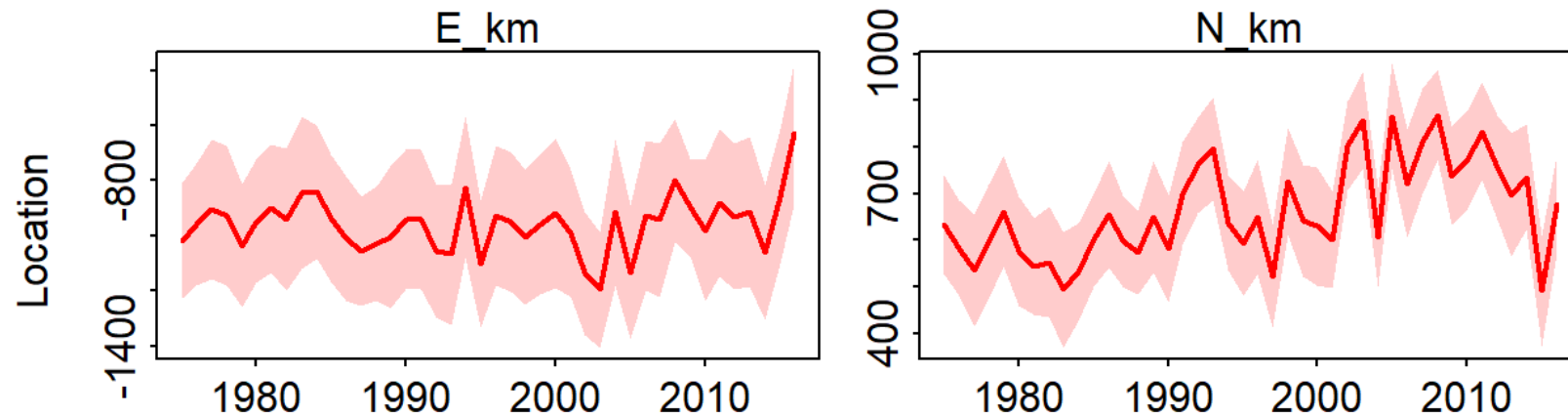
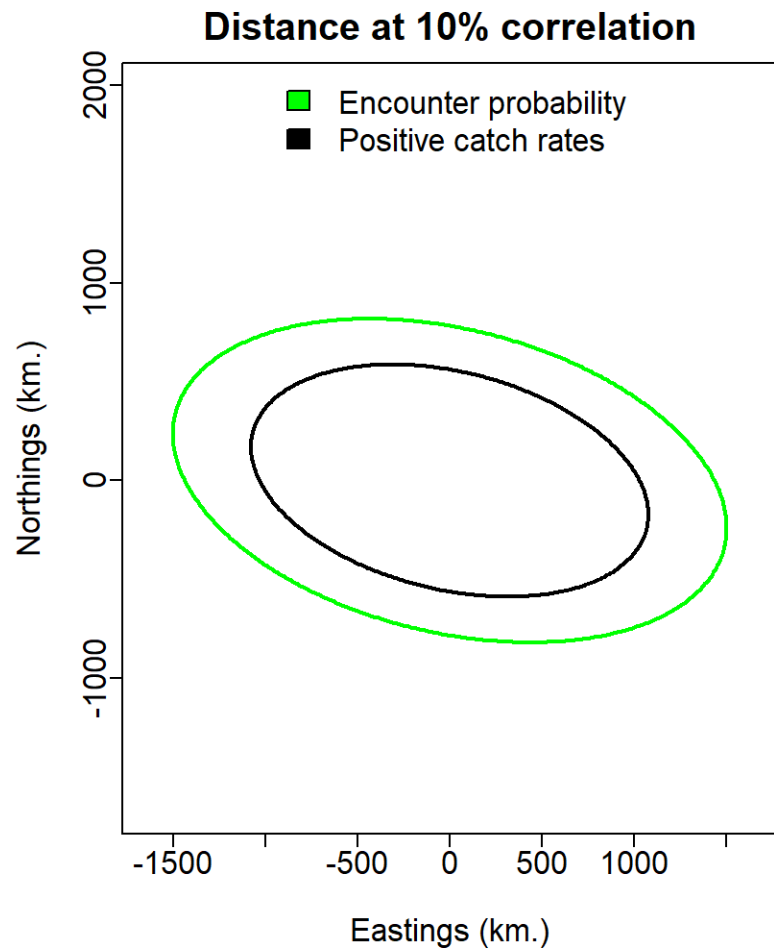
# Step 3. Compute index of abundance and CV



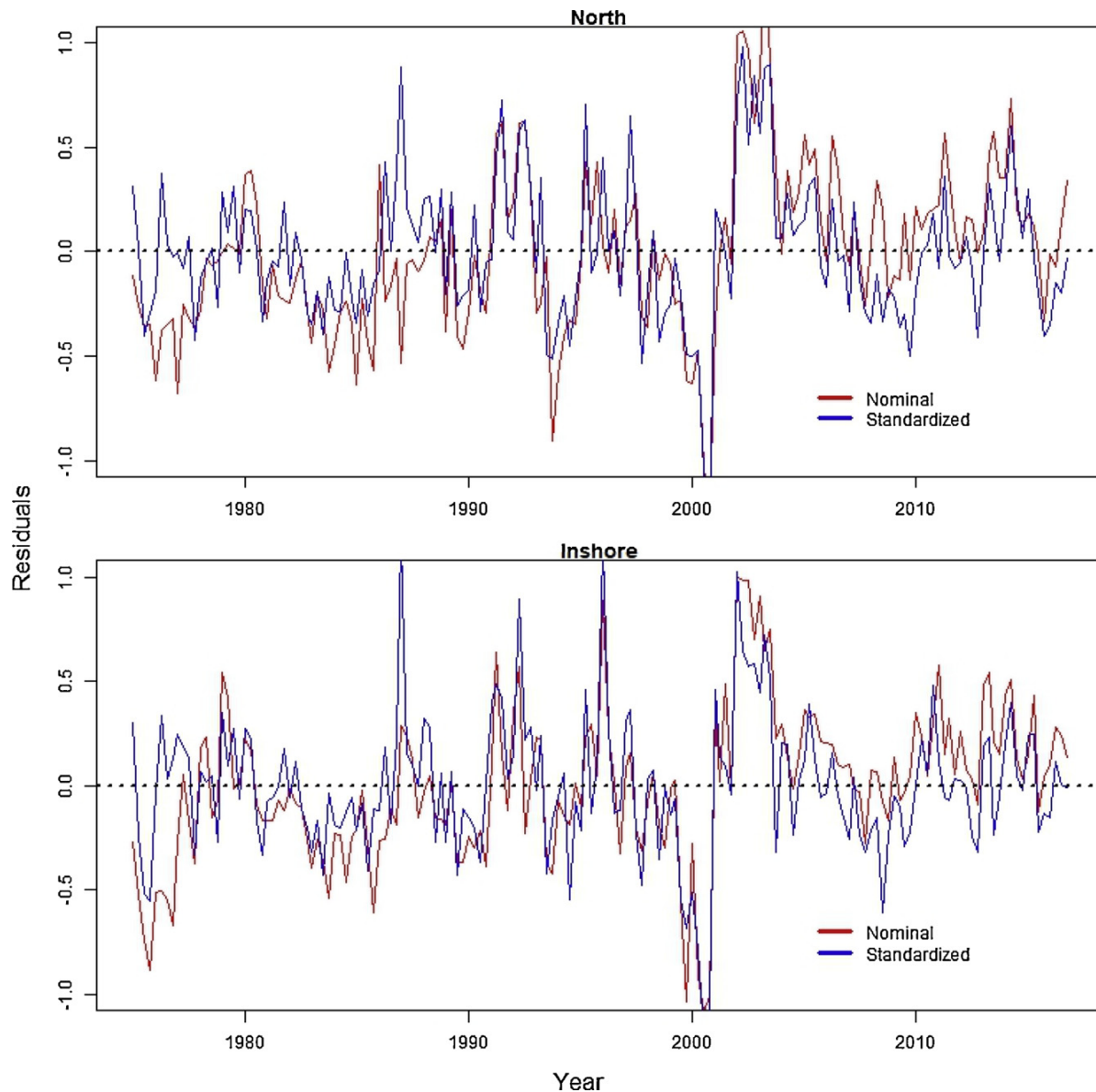
# Step 4. Diagnostics



# Step 5. Derived Quantities from VAST

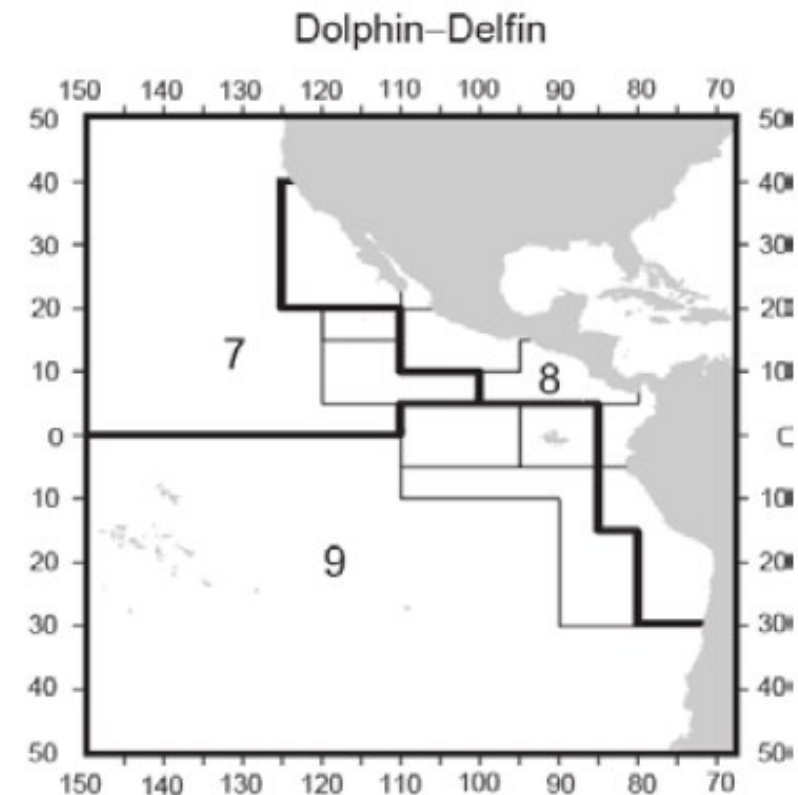


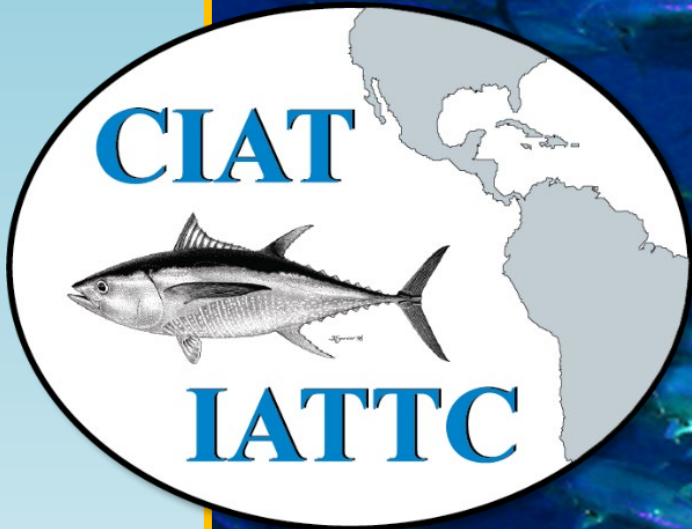
# Step 6. Use the standardized index in the assessment



**Using the standardized index can improve the stock assessment:**

- reduced residual pattern
- 79.27 units increase in log-likelihood





Thank you!

